

Cambridge Assessment International Education Cambridge International General Certificate of Secondary Education

#### MATHEMATICS (US)

0444/43 October/November 2017

Paper 4 (Extended) MARK SCHEME Maximum Mark: 130

Published

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# Cambridge IGCSE – Mark Scheme PUBLISHED

#### Abbreviations

cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
SC	Special Case
nfww	not from wrong working

soi seen or implied

Question	Answer	Marks	Partial Marks
1(a)(i)	$180 \div (2+3+5) \times 5 = 90$	1	with no errors seen
1(a)(ii)	7.05 or 7.053	3	M2 for $\frac{x}{12} = \sin 36$ oe or better or B1 for 36 or 54 seen
1(b)(i)	13	2	<b>M1</b> for 7.8 ÷ 3 soi
1(b)(ii)	36.9 or 36.86 to 36.87	3	<b>B1</b> for smallest angle identified <b>M1</b> for sin[] = $\frac{3}{5}$ oe or sin[] = $\frac{7.8}{their \mathbf{b}(\mathbf{i})}$ oe If zero scored, <b>SC1</b> for calculation of 53.1
2(a)	343	1	
2(b)(i)	1	1	
2(b)(ii)	$x^{10}$ final answer	1	
2(b)(iii)	$9x^{16}$ final answer	2	<b>B1</b> for $x^{12}$ or $x^{16}$ or $(3x^8)^2$ seen
2(c)(i)	2(x-3)(x+3) final answer	2	M1 for $(2x+6)(x-3)$ or $(2x-6)(x+3)$ or $(x-3)(x+3)$
2(c)(ii)	$\frac{2(x+3)}{x+10}$ or $\frac{2x+6}{x+10}$ final answer nfww	3	M2 for $(x + 10)(x - 3)$ or M1 for $(x + a)(x + b)$ where $ab = -30$ or $a + b = 7$
3(a)	480	3	M2 for $456 \div \left(1 - \frac{5}{100}\right)$ oe or M1 for associating 456 with 95%
3(b)	261.47	2	<b>M1</b> for $200 \times \left(1 + \frac{1.5}{100}\right)^{18}$

Question	Answer	Marks	Partial Marks
3(c)	1.2	3	<b>M2</b> for $\sqrt[17]{\frac{2449.62}{2000}}$ oe, soi by 1.012[0] or <b>M1</b> for $\frac{2449.62}{2000}$ or $2000 \times ()^{17} = 2449.62$
3(d)	$c - \frac{cp}{100}$ oe	2	<b>M1</b> for $\frac{cp}{100}$ seen
4(a)	$80 < t \leqslant 100$	1	
4(b)	86 nfww	4	M1 for midpoints soi
			<b>M1</b> for use of $\Sigma fx$ with x in correct interval including both boundaries
			<b>M1</b> (dep on 2nd <b>M1</b> ) for $\Sigma fx \div 150$
4(c)(i)	Reference to not knowing the individual values so we do not know the highest or the lowest values	1	
4(c)(ii)	62.4	2	<b>M1</b> for 26 ÷ 150 or 360 ÷ 150
4(d)	$\frac{22}{150}$ oe	1	
4(e)(i)	$\frac{90}{22350}$ oe	2	M1 for $\frac{10}{150} \times \frac{9}{149}$ After zero scored, SC1 for answer $\frac{100}{22500}$ oe
4(e)(ii)	$\frac{440}{22350}$ oe	3	M2 for $\frac{10}{150} \times \frac{22}{149} + \frac{22}{150} \times \frac{10}{149}$ oe or M1 for $\frac{10}{150} \times \frac{22}{149}$ or $\frac{22}{150} \times \frac{10}{149}$ oe After zero scored, SC1 for answer $\frac{440}{22500}$ oe
4(f)	13, 8.5, 7.25, 1.1	3	<b>B2</b> for 3 correct or <b>B1</b> for 1 correct or for 3 correct FD.s 5.2, 3.4, 2.9, 0.44 oe

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Question	Answer	Marks	Partial Marks
5(a)(i)	Image at (0, 1), (0, 2), (-3, 1)	2	<b>B1</b> for reflection in $y = 0$ or $x = k$
5(a)(ii)	Image at $(0, 0), (0, -2), (6, -2)$	2	<b>B1</b> for correct size and correct orientation wrong position or for 2 correct vertices plotted
5(a)(iii)	Image at (-5, 4), (-5, 5), (-2, 4)	2	<b>B1</b> for translation by $\begin{pmatrix} -5\\k \end{pmatrix}$ or $\begin{pmatrix} k\\3 \end{pmatrix}$
5(b)	Rotation 90° clockwise oe (4, -1)	3	B1 for each
6(a)	-7	1	
6(b)	5 - 2x	2	<b>M1</b> for $2(3-x) - 1$
6(c)(i)	$\frac{4}{3}$ oe	2	<b>M1</b> for $2x - 1 = 3 - x$
6(c)(ii)	-3	1	
6(d)	$\frac{x+1}{2}$ of final answer	2	<b>M1</b> for $x = 2y - 1$ or $y + 1 = 2x$ or $\frac{y}{2} = x - \frac{1}{2}$
6(e)	$\frac{3x-2}{x}$ final answer	2	<b>M1</b> for $3-\frac{2}{x}$
6(f)	16	1	
7(a)(i)	25.5 or 25.46	2	<b>M1</b> for $\pi \times 5^2 \times h = 2000$ oe
7(a)(ii)	9.85 or 9.847	3	M2 for $[r^3=] 2000 \div \left(\frac{2}{3}\pi\right)$ oe or M1 for $\frac{2}{3}\pi r^3 = 2000$ oe
7(a)(iii)	952 or 952.4	3	M2 for $[6 \times] \sqrt[3]{2000}^2$ or M1 for $\sqrt[3]{2000}$ or 6 times <i>their</i> area of one face
7(b)(i)	22.5 or 22.49	2	<b>M1</b> for $\frac{1}{2} \times 7 \times 10 \times \sin 40$
7(b)(ii)	$\sqrt{(10^2 + 7^2 - 2 \times 10 \times 7 \cos 40)} + 7 + 10$	M3	M2 for $10^2 + 7^2 - 2 \times 10 \times 7 \cos 40$ or M1 for correct implicit cosine rule
	23.46	A2	A1 for 6.46 or 41.7 to 41.8

Question	Answer	Marks	Partial Marks
7(c)	64.9 or 64.92 to 64.94	3	M2 for $28.2 - 2 \times 9 = \frac{c}{360} \times 2 \times \pi \times 9$ oe or M1 for $\frac{c}{360} \times 2 \times \pi \times 9$ soi
8(a)	9, -6, 9	3	B1 for each
8(b)	Correct graph	4	<b>B3FT</b> for 6 or 7 correct points or <b>B2FT</b> for 4 or 5 correct points or <b>B1FT</b> for 2 or 3 correct points
8(c)	-3.5 to -3.35 and 0.8 to 0.9	<b>2</b> FT	FT <i>their</i> graph B1FT for either
8(d)	$a = \frac{5}{4} \text{ or } 1\frac{1}{4} \text{ or } 1.25$ $b = -\frac{49}{8} \text{ or } -6\frac{1}{8} \text{ or } -6.125$	3	<b>B2</b> for either correct or <b>M1</b> for $[2]\left(x+\frac{5}{4}\right)^2$ seen isw or for $2x^2 + 4ax + 2a^2 + b$
9(a)(i)	5	1	
9(a)(ii)	$-\frac{3}{2}$ oe	1	
9(b)	$\left(\frac{4}{5}, 0\right)$ oe	2	<b>M1</b> for $5x - 4 = 0$ soi
9(c)	y = -0.2x + 11 final answer	4	M2 for $y = -0.2x + b$ oe (any form) FT <i>their</i> (a) or B1FT for grad = $\frac{-1}{their(a)(i)}$ soi and M1 for substitution of (10, 9) into <i>their</i> equation
9(d)	(2, 6)	3	M1 for elimination of one variable A1 for $x = 2$ or $y = 6$
9(e)	13 oe	3	<b>M2</b> for $(4+9) \times their 2 \div 2$ oe or <b>B1</b> for 9 oe or 4 or -4 seen

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Question	Answer	Marks	Partial Marks
10(a)	$\frac{10}{x-0.5}$ final answer	1	Accept $\frac{20}{2x-1}$
10(b)(i)	$\frac{10}{x - 0.5} - \frac{10}{x} = 0.25 \text{ oe}$	M1	FT their (a)
	10x - 10(x - 0.5) = 0.25x (x - 0.5) oe	M1	Clears algebraic denominators or collects as a single fraction FT <i>their</i> algebraic fractions dep on two fractions with algebraic denominators
	$10x - 10x + 5 = 0.25x^2 - 0.125x \text{ or}$ better	B1	Expands brackets
	$2x^2 - x - 40 = 0$	A1	Dep on M1M1B1 and no errors seen
10(b)(ii)	$\frac{-1\pm\sqrt{(-1)^2-4\times2\times-40}}{2\times2}$ oe	B2	<b>B1</b> for $\sqrt{(-1)^2 - 4(2)(-40)}$ or better
	2×2		or <b>B1</b> for $\frac{1+\sqrt{q}}{2\times 2}$ or $\frac{1-\sqrt{q}}{2\times 2}$ or both
	-4.23 and 4.73 final answers	B1B1	<b>SC1</b> for -4.229 <b>and</b> 4.729 or for -4.23 <b>and</b> 4.73 seen in working or for -4.73 <b>and</b> 4.23 as final answer or for -4.2 or -4.22 <b>and</b> 4.7 or 4.72 as final answer
10(b)(iii)	2 [hours] 7 [minutes]	3	<b>B2</b> for 2.11 or 2.114 to 2.115 or 126.8 to 126.9 or 127 or <b>M1</b> for 10 ÷ <i>their</i> positive root from ( <b>b</b> )(ii)
11(a)(i)	$2^2 \times 3^2 \times 5$ oe	2	M1 for 3 correct prime factors in a tree or table seen before the first error or for 2, 3, 5 identified
11(a)(ii)	540	2	M1 for $2^2 \times 3^3 \times 5$ or $2 \times 3^3$ shown or answer $540k$
11(b)	X = 8575	4	<b>B3</b> for $X = 8575$ or $Y = 6125$
	<i>Y</i> = 6125		or <b>B2</b> for $a = 5$ or $b = 1$ soi or <b>B1</b> for $1225 = 5^2 \times 7^2$ or $42875 = 5^3 \times 7^3$ or <b>M1</b> for $a^2 \times 7^2$ [= 1225] or $a^3 \times 7^{b+2}$ [= 42 875]